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Forecasting the Euro: Do Forecasters Have an Asymmetric Loss Function?

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Abstract

Based on the approach advanced by Elliott et al. (Rev. Ec. Studies. 72, 1197–1125, 2005), we analyzed whether the loss function of a sample of exchange rate forecasters is asymmetric in the forecast error. Using forecasts of the euro/dollar exchange rate, we found that the shape of the loss function varies across forecasters. Our empirical results suggest that it is important to account for the heterogeneity of exchange rate forecasts at the microeconomic level of individual forecasters when one seeks to analyze whether forecasters form exchange rate forecasts under an asymmetric loss function.

JEL classification: F31, D84

Keywords: Exchange rate; Forecasting; Loss function

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1 Introduction

Because the way agents form their exchange rate forecasts plays a key role in modern models of exchange rate determination, much empirical research has been done to recover important characteristics of exchange rate forecasts. Many researchers have reported that one important characteristic of exchange rate forecasts is that they are not consistent with traditional criteria of forecast rationality (for a classic contribution, see Ito 1990). Another important characteristic of exchange rate forecasts is that a substantial degree of heterogeneity becomes apparent at the microeconomic level when one analyzes forecasts of individual forecasters (MacDonald and Marsh 1996, Benassy-Quere et al. 2003).

Traditional criteria of forecast rationality assume that forecasters have a symmetric and quadratic loss function. Assuming a quadratic loss function, however, may be problematic. In fact, recent research has provided evidence indicating that deviations from a quadratic loss function are quite common (see Elliott et al. (2005) for OECD and IMF forecasts, Christodoulakis and Mamatzakis (2008a) for forecasts of the European Commission, and Boero et al. (2008) for inflation forecasts). With regard to exchange rates, Christodoulakis and Mamatzakis (2008a) find that an asymmetric loss function may be better suited for the analysis of foreign exchange markets than a traditional symmetric loss function. They derive their finding using the forward exchange rate to measure exchange rate forecasts. The forward exchange rate, however, summarizes the market-wide exchange rate forecast and thus neglects the potentially important heterogeneity of exchange rate forecasts at the microeconomic level.

We used survey data on euro/dollar forecasts to recover potential asymmetries of forecasters' loss function at the microeconomic level. For a sample of more than 8,500 forecasts, we found that forecasters on average tend to incur higher losses when they underpredict the exchange rate than when they overpredict the exchange rate. For pooled data, this evidence in favor of an asymmetric loss function is stronger for twelve-months-ahead forecasts than for one-month-ahead forecasts, though the differences across forecast horizons are small for pooled data. At the microeconomic level, the shape of the loss function varies to a substantial extent across forecasters, where some forecasters seem to incur high losses when they overpredict the euro/dollar exchange rate, whilst other forecasters incur high losses when they underpredict the exchange rate. Many forecasters, however, deliver forecasts that are consistent with a symmetric loss function. Furthermore, there appears no clear-cut link between the shape of forecasters' loss function and the length of the forecast horizon. Christodoulakis and Mamatzakis (2008b), in contrast, report that, when one uses the forward rate to measure market-wide exchange rate forecasts, the loss function becomes more symmetric as the forecast horizon gets shorter. Results based on exchange rate forecasts at the microeconomic level, thus, might differ from results derived from market-wide exchange rate forecasts.

In order to analyze the shape of forecasters' loss function, we used an approach recently developed by Elliott et al. (2005), which has also been studied by Christodoulakis and Mamatzakis (2008b). This approach is easy to implement, it informs about the type of a potential asymmetry in forecasters' loss function, and it allows the rationality of forecasts under an asymmetric loss function to be tested. In Section 2, we briefly outline the approach developed by Elliott et al. (2005). In Section 3, we describe our data and our empirical

results. In Section 4, we offer some concluding remarks.

2 Theoretical Background

The approach developed by Elliott et al. (2005) rests on the assumption that a forecaster's loss function, \mathcal{L} can be described in terms of the following general functional form:

$$\mathcal{L} = [\alpha + (1 - 2\alpha)I(s_{t+1} - f_{t+1} < 0)]|s_{t+1} - f_{t+1}|^p, \quad (1)$$

where s_{t+1} denotes the realization of the exchange rate, f_{t+1} , denotes the forecast formed in period t of the realization of the exchange rate in period $t + 1$, I denotes the indicator function, $p = 1$ for a lin-lin loss function and $p = 2$ for a quad-quad loss function, and $\alpha \in (0, 1)$ governs the degree of asymmetry of the loss function. In the case of $\alpha = 0.5$, the loss function is symmetric. For $\alpha = 0.5$ and $p = 2$, the loss a forecaster increases in the squared forecast error. For $\alpha = 0.5$ and $p = 1$, the loss increases in the absolute forecast error.

Elliott et al. (2005) show that, for a given parameter p , which defines the general functional form of the loss function, the asymmetry parameter, α , can be consistently estimated as

$$\hat{\alpha} = \frac{\left[\frac{1}{T} \sum_{t=\tau}^{T+\tau-1} v_t |s_{t+1} - f_{t+1}|^{p-1} \right]' \hat{S}^{-1} \left[\frac{1}{T} \sum_{t=\tau}^{T+\tau-1} v_t I(s_{t+1} - f_{t+1} < 0) |s_{t+1} - f_{t+1}|^{p-1} \right]}{\left[\frac{1}{T} \sum_{t=\tau}^{T+\tau-1} v_t |s_{t+1} - f_{t+1}|^{p-1} \right]' \hat{S}^{-1} \left[\frac{1}{T} \sum_{t=\tau}^{T+\tau-1} v_t |s_{t+1} - f_{t+1}|^{p-1} \right]}, \quad (2)$$

where $\hat{S} = \frac{1}{T} \sum_{t=\tau}^{T+\tau-1} v_t v_t' (I(s_{t+1} - f_{t+1} < 0) - \hat{\alpha})^2 |s_{t+1} - f_{t+1}|^{2p-2}$ denotes a weighting matrix, v_t denotes a vector of instruments, T denotes the number of forecasts available, starting at $t = \tau + 1$. Because the weighting matrix depends on $\hat{\alpha}$, estimation is done iteratively. Testing whether $\hat{\alpha}$ differs from α_0 is done by using the following z-test $\sqrt{T}(\hat{\alpha} - \alpha_0) \rightarrow \mathcal{N}(0, (\hat{h}' \hat{S}^{-1} \hat{h})^{-1})$, where $\hat{h} = \frac{1}{T} \sum_{t=\tau}^{T+\tau-1} v_t |s_{t+1} - f_{t+1}|^{p-1}$.

We considered as instruments a constant (Model 1), and a constant and lagged exchange rate (Model 2). Because the survey data that we shall describe in Section 3 below contains forecasts for an unbalanced panel of forecasters, we did not follow Elliott et al. (2005) in using lagged published forecasts as another instrument.

Testing whether $\hat{\alpha}$ differs from α_0 is done by using the following z-test $\sqrt{T}(\hat{\alpha} - \alpha_0) \rightarrow \mathcal{N}(0, (\hat{h}' \hat{S}^{-1} \hat{h})^{-1})$, where $\hat{h} = \frac{1}{T} \sum_{t=\tau}^{T+\tau-1} v_t |s_{t+1} - f_{t+1}|^{p-1}$. Elliott et al. (2005) further prove that a test for rationality of forecasts, given a loss function of the lin-lin or a quad-quad type ($p = 1, 2$), can be performed by computing

$$J(\hat{\alpha}) = \frac{1}{T} \left(x_t' \hat{S}^{-1} x_t \right) \sim \chi_{d-1}^2, \quad (3)$$

where $x_t = \sum_{t=\tau}^{T+\tau-1} v_t [I(s_{t+1} - f_{t+1} < 0) - \hat{\alpha}] |s_{t+1} - f_{t+1}|^{p-1}$ and d denotes the number of instruments. In the case of a symmetric loss function, the rationality test is given by $J(0.5) \sim \chi_d^2$. The statistic $J(0.5)$ answers the question of whether forecasters under the maintained assumption of a symmetric loss function form rational exchange rate forecasts. The statistic $J(\hat{\alpha})$, answers the question of whether forecasters form rational forecasts, given an estimated (unconstrained) asymmetric loss function (lin-lin or quad-quad). A

comparison of $J(\hat{\alpha})$ with $J(0.5)$ shows whether an asymmetric loss function helps to remedy a potential failure of rationality of forecasts observed under a symmetric loss function.

3 Empirical Analysis

In order to recover, at the microeconomic level, a potential asymmetry in forecasters' loss function, we used survey data on one-month-ahead, three-months-ahead, and twelve-months-ahead forecasts of the euro/dollar exchange rate compiled by Consensus Forecasts Inc. The survey data contain information on individual exchange rate forecasts issued by forecasters who work for institutions such as investment banks, large international corporations, economic research institutes, and at universities. Because not all forecasters participated in all surveys, the survey data are available in the form of an unbalanced panel. In our empirical analysis, we only considered forecasters who participated at least 20 times in the survey (31 forecasters). The survey data are available at a monthly frequency for the period 1999/1–2011/7. In total, we could use 2,927 one-month-ahead forecasts, 2,940 three-months-ahead forecasts, and 2,747 twelve-months-ahead forecasts.

– Please insert Figure 1 about here. –

Figure 1 illustrates the properties of the data. We used the program R to compute this figure and all other results documented in this paper (R Development Core Team 2010).

The figure shows that the cross-sectional average of forecasts (solid line) across individual forecasts closely tracked the euro/dollar exchange rate (dashed line). More interesting is the shaded area, which highlights that, at the microeconomic level, individual forecasts showed a substantial degree of cross-forecaster heterogeneity. The shaded area is defined as the cross-sectional range between the maximum and the minimum exchange rate forecast. Given the heterogeneity of forecasts, one would expect a substantial extent of cross-sectional variation in the asymmetry parameter, $\hat{\alpha}$, across forecasters.

– Please include Table 1 about here. –

Table 1 summarizes the results of a Wilcoxon test of the null hypothesis that the distribution of forecast errors is symmetric around zero. Again, a substantial cross-sectional variation becomes evident. While for some forecasters the null hypothesis cannot be rejected, a symmetric distribution seems to fit the forecast errors made by other forecasters less well. The test results are significant for forecasters 5, 15, 19, 28, 30, and 31 in the case of one-month-ahead forecasts, suggesting that these forecasters may form forecasts under an asymmetric loss function. Similarly, for three-months-ahead forecasts and twelve-months-ahead forecasts, the results of a Wilcoxon test (not reported for the sake of brevity) also yield evidence of an asymmetric distribution of forecast errors for some forecasters, but not for others. We, thus, expect also for longer term forecasts a substantial cross-sectional heterogeneity with respect to the shape of forecasters' loss function.

– Please include Table 2 about here. –

Table 2 presents results for pooled data to alleviate a comparison of our results with the results documented by Christodoulakis and Mamatzakis (2008b). The point estimates of the asymmetry parameter, $\hat{\alpha}$, tend to become smaller as the forecasting horizon gets longer. The differences across forecast horizons, however, appear to be small and statistically insignificant. The weak link between the magnitude of the estimates of the asymmetry parameter, $\hat{\alpha}$, and the length of the forecasting horizon is in contrast to results reported by Christodoulakis and Mamatzakis (2008b). Using forward exchange rates to measure market-wide forecasts of the euro/dollar exchange rate, they report $\hat{\alpha} = 0.4207$ for weekly data and $\hat{\alpha} = 0.3860$ for monthly data in case of a lin-lin loss function. For a quad-quad loss function, they report $\hat{\alpha} = 0.4089$ for weekly data and $\hat{\alpha} = 0.2846$ for monthly data. Their results thus imply that the point estimates of the asymmetry parameter of the loss function become significantly smaller as the forecast horizon increases, implying that the asymmetry of the loss function gets more pronounced for longer forecasting horizons.

– Please include Table 3–5 about here. –

Tables 3–5 summarize, for every forecaster, the estimates of the asymmetry parameter, $\hat{\alpha}$, the corresponding standard error, and the z-test of the null hypothesis $\hat{\alpha} = \alpha_0 = 0.5$. The loss function is of the lin-lin type. The results for a quad-quad loss function are similar. They are not reported but available upon request. The general message conveyed by the estimates of the asymmetry parameter, $\hat{\alpha}$, is that there is quite some heterogeneity across forecasters with respect to the shape of the loss function, irrespective of whether one uses a lin-lin loss function or a quad-quad loss function. Many forecasters deliver forecasts that

are consistent with a symmetric loss function. Furthermore, there appears no clear-cut link between the shape of forecasters' loss function and the length of the forecast horizon.

– Please include Table 6 about here. –

Table 6 summarizes the results of the J test of forecast rationality for pooled data. Again, we present the results for the pooled data to make it easy for a reader to compare our results with the results documented by Christodoulakis and Mamatzakis (2008b). Assuming an asymmetric loss function tends to lead to a nonrejection of the hypothesis of rational forecasts for twelve-months-ahead forecasts, but the results depend on whether one assumes a lin-lin loss function or a quad-quad loss function.

– Please include Table 7–9 about here. –

Tables 7–9 summarize the results we obtained when we studied at the microeconomic level the forecasts of individual forecasters. The results shown in the tables are for a lin-lin loss function (the results for a quad-quad loss function are similar and available upon request). For many forecasters, the hypothesis of rational forecasts cannot be rejected, irrespective of the symmetry or asymmetry of the assumed loss function. For a few forecasters, the assumption of an asymmetric loss function makes their forecasts look rational. For other forecasters, however, forecast rationality can be rejected irrespective of the assumed loss function.

Those forecasters for which the J-test yields results in a rejection of forecast rationality irrespective of the assumed loss function may indeed form irrational forecasts that are not orthogonal to information in their information set. Another possibility, however, is that these forecasters form rational forecasts, but that the process of forecasting the euro/dollar exchange rate is more complex than implied by the lin-lin (or the quad-quad) loss function. For example, strategic interactions among forecasters may lead forecasters to publish forecasts that intentionally deviate from the forecasts of others. Empirical evidence of such “anti-herding” of exchange rate forecasters has been reported by Pierdzioch and Stadtmann (2011). If forecasters anti-herd, their loss function is likely to deviate from a simple symmetric (quadratic) loss function (Laster et al. 1999) and, thus, rational forecasts violate traditional rationality criteria, which are based on a quadratic loss function. If anti-herding, however, reflects deviations from a symmetric loss function, it is not necessarily the case that a loss function of the lin-lin or the quad-quad form suffice to fully account for such deviations.

4 Concluding Remarks

Our empirical results suggest that it is important to account for the heterogeneity of exchange rate forecasts at the microeconomic level of individual forecasters when one seeks to analyze whether individual forecasters form exchange rate forecasts under an asymmetric loss function. As for the loss function of a “representative” forecaster, the analysis of pooled data or forward rates as measures of market-wide exchange rate expectations is

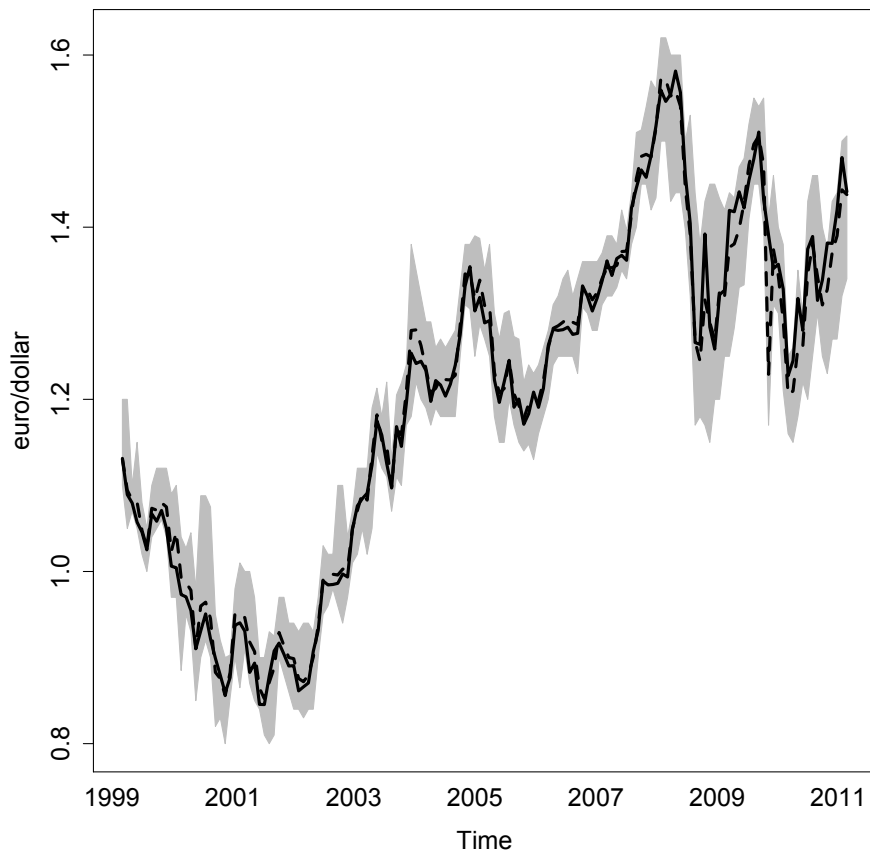
likely to provide important insights. Our results, however, suggest that studying market-wide information to recover the shape of the loss function of individual forecasters is likely to cloud a substantial cross-sectional heterogeneity with respect to the shape of the loss function at the microeconomic level. While the assumption of a representative forecaster often suffices to set up macroeconomic models of exchange rate determination, our results imply that, when researchers seek to test behavioral theories of exchange rate dynamics, accounting for the cross-sectional heterogeneity of forecasters can help to recover, at least when the euro/dollar exchange rate is being studied, interesting new phenomena.

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Figure 1: The Data



Note: The solid line shows the exchange rate. The dashed line shows the (lagged) cross-sectional mean forecast. The shaded area shows the range of forecasts.

Table 1: Results of the Wilcoxon Test (One-Month-Ahead Forecasts)

| No. | Obs. | Test | p-value |
|-----|------|------|---------|
| 1 | 119 | 3138 | 0.2525 |
| 2 | 104 | 3009 | 0.3665 |
| 3 | 144 | 5251 | 0.9515 |
| 4 | 129 | 3653 | 0.2052 |
| 5 | 39 | 510 | 0.0957 |
| 6 | 26 | 204 | 0.4834 |
| 7 | 21 | 109 | 0.8382 |
| 8 | 79 | 1714 | 0.5141 |
| 9 | 147 | 4969 | 0.3639 |
| 10 | 107 | 2947 | 0.8582 |
| 11 | 129 | 3776 | 0.3281 |
| 12 | 57 | 939 | 0.3735 |
| 13 | 140 | 5287 | 0.4647 |
| 14 | 96 | 2354 | 0.9258 |
| 15 | 140 | 4071 | 0.0725 |
| 18 | 137 | 4721 | 0.9914 |
| 19 | 132 | 3407 | 0.0258 |
| 20 | 133 | 3991 | 0.2974 |
| 21 | 111 | 3203 | 0.7810 |
| 23 | 106 | 3249 | 0.1930 |
| 24 | 139 | 4819 | 0.9238 |
| 25 | 146 | 4830 | 0.2959 |
| 26 | 124 | 4276 | 0.3179 |
| 27 | 66 | 912 | 0.2176 |
| 28 | 132 | 5290 | 0.0408 |
| 29 | 144 | 5138 | 0.8709 |
| 30 | 27 | 265 | 0.0692 |
| 31 | 23 | 201 | 0.0563 |

Note: The null hypothesis is that the distribution of forecast errors is symmetric around zero.

Table 2: Results for pooled data

Panel A: One-month-ahead forecasts, lin-lin loss function

| No. | Obs. | $\hat{\alpha}_{Model1}$ | se | z-test | $\hat{\alpha}_{Model2}$ | se | z-test |
|-----|------|-------------------------|--------|--------|-------------------------|--------|--------|
| All | 2927 | 0.5091 | 0.0092 | 0.9798 | 0.5091 | 0.0092 | 0.9877 |

Panel B: Three-months-ahead forecasts, lin-lin loss function

| No. | Obs. | $\hat{\alpha}_{Model1}$ | se | z-test | $\hat{\alpha}_{Model2}$ | se | z-test |
|-----|------|-------------------------|--------|--------|-------------------------|--------|---------|
| All | 2940 | 0.4803 | 0.0092 | -2.141 | 0.48 | 0.0092 | -2.1659 |

Panel C: Twelve-months-ahead forecasts, lin-lin loss function

| No. | Obs. | $\hat{\alpha}_{Model1}$ | se | z-test | $\hat{\alpha}_{Model2}$ | se | z-test |
|-----|------|-------------------------|--------|---------|-------------------------|--------|--------|
| All | 2747 | 0.4751 | 0.0095 | -2.6172 | 0.4751 | 0.0095 | -2.618 |

Panel D: One-month-ahead forecasts, quad-quad loss function

| No. | Obs. | $\hat{\alpha}_{Model1}$ | se | z-test | $\hat{\alpha}_{Model2}$ | se | z-test |
|-----|------|-------------------------|--------|---------|-------------------------|--------|--------|
| All | 2927 | 0.4958 | 0.0123 | -0.3458 | 0.5018 | 0.0121 | 0.1511 |

Panel E: Three-months-ahead forecasts, quad-quad loss function

| No. | Obs. | $\hat{\alpha}_{Model1}$ | se | z-test | $\hat{\alpha}_{Model2}$ | se | z-test |
|-----|------|-------------------------|--------|--------|-------------------------|--------|--------|
| All | 2940 | 0.5007 | 0.0117 | 0.0571 | 0.5058 | 0.0115 | 0.5045 |

Panel F: Twelve-months-ahead forecasts, quad-quad loss function

| No. | Obs. | $\hat{\alpha}_{Model1}$ | se | z-test | $\hat{\alpha}_{Model2}$ | se | z-test |
|-----|------|-------------------------|--------|---------|-------------------------|--------|---------|
| All | 2747 | 0.4889 | 0.0114 | -0.9715 | 0.4874 | 0.0114 | -1.1032 |

Note: se = standard error, z-test = test of the null hypothesis that $\hat{\alpha} = 0.5$. The instruments used are the following: a constant (Model 1), a constant and the lagged exchange rate (Model 2).

Table 3: Asymmetry parameter, lin-lin loss function, one-month-ahead forecasts

| No. | Obs. | $\hat{\alpha}_{Model1}$ | se | z-test | $\hat{\alpha}_{Model2}$ | se | z-test |
|-----|------|-------------------------|--------|---------|-------------------------|--------|---------|
| 1 | 119 | 0.5630 | 0.0455 | 1.3861 | 0.5632 | 0.0455 | 1.3905 |
| 2 | 104 | 0.4808 | 0.0490 | -0.3925 | 0.4799 | 0.0490 | -0.4094 |
| 3 | 144 | 0.4653 | 0.0416 | -0.8354 | 0.4653 | 0.0416 | -0.8357 |
| 4 | 129 | 0.5736 | 0.0435 | 1.6913 | 0.5737 | 0.0435 | 1.6916 |
| 5 | 39 | 0.3590 | 0.0768 | -1.8360 | 0.3584 | 0.0768 | -1.8442 |
| 6 | 26 | 0.4615 | 0.0978 | -0.3934 | 0.4594 | 0.0977 | -0.4159 |
| 7 | 21 | 0.6667 | 0.1029 | 1.6202 | 0.7443 | 0.0952 | 2.5663 |
| 8 | 79 | 0.5063 | 0.0562 | 0.1125 | 0.5064 | 0.0562 | 0.1143 |
| 9 | 147 | 0.5238 | 0.0412 | 0.5780 | 0.5241 | 0.0412 | 0.5840 |
| 10 | 107 | 0.5140 | 0.0483 | 0.2901 | 0.5142 | 0.0483 | 0.2937 |
| 11 | 129 | 0.5349 | 0.0439 | 0.7943 | 0.5381 | 0.0439 | 0.8680 |
| 12 | 57 | 0.4737 | 0.0661 | -0.3979 | 0.4736 | 0.0661 | -0.3997 |
| 13 | 140 | 0.4714 | 0.0422 | -0.6772 | 0.4713 | 0.0422 | -0.6813 |
| 14 | 96 | 0.4583 | 0.0509 | -0.8193 | 0.4582 | 0.0509 | -0.8211 |
| 15 | 140 | 0.5429 | 0.0421 | 1.0179 | 0.5476 | 0.0421 | 1.1325 |
| 18 | 137 | 0.4818 | 0.0427 | -0.4275 | 0.4817 | 0.0427 | -0.4285 |
| 19 | 132 | 0.5985 | 0.0427 | 2.3082 | 0.5985 | 0.0427 | 2.3083 |
| 20 | 133 | 0.5714 | 0.0429 | 1.6646 | 0.5720 | 0.0429 | 1.6779 |
| 21 | 111 | 0.4685 | 0.0474 | -0.6657 | 0.4585 | 0.0473 | -0.8768 |
| 23 | 106 | 0.4340 | 0.0481 | -1.3718 | 0.4331 | 0.0481 | -1.3908 |
| 24 | 139 | 0.5180 | 0.0424 | 0.4244 | 0.5181 | 0.0424 | 0.4280 |
| 25 | 146 | 0.5616 | 0.0411 | 1.5011 | 0.5652 | 0.0410 | 1.5902 |
| 26 | 124 | 0.4758 | 0.0448 | -0.5394 | 0.4754 | 0.0448 | -0.5480 |
| 27 | 66 | 0.5455 | 0.0613 | 0.7416 | 0.5464 | 0.0613 | 0.7575 |
| 28 | 132 | 0.4242 | 0.0430 | -1.7611 | 0.4239 | 0.0430 | -1.7685 |
| 29 | 144 | 0.5139 | 0.0417 | 0.3335 | 0.5139 | 0.0417 | 0.3340 |
| 30 | 27 | 0.2963 | 0.0879 | -2.3180 | 0.2748 | 0.0859 | -2.6212 |
| 31 | 23 | 0.3043 | 0.0959 | -2.0392 | 0.2737 | 0.0930 | -2.4338 |

Note: se = standard error, z-test = test of the null hypothesis that $\hat{\alpha} = 0.5$. The instruments used are the following: a constant (Model 1), a constant and the lagged exchange rate (Model 2).

Table 4: Asymmetry parameter, lin-lin loss function, three-months-ahead forecasts

| No. | Obs. | $\hat{\alpha}_{Model1}$ | se | z-test | $\hat{\alpha}_{Model2}$ | se | z-test |
|-----|------|-------------------------|--------|---------|-------------------------|--------|----------|
| 1 | 117 | 0.5470 | 0.0460 | 1.0215 | 0.5478 | 0.0460 | 1.0387 |
| 2 | 114 | 0.5000 | 0.0468 | 0.0000 | 0.5000 | 0.0468 | 0.0000 |
| 3 | 142 | 0.4437 | 0.0417 | -1.3513 | 0.4422 | 0.0417 | -1.3868 |
| 4 | 127 | 0.5433 | 0.0442 | 0.9798 | 0.5433 | 0.0442 | 0.9805 |
| 6 | 24 | 0.2917 | 0.0928 | -2.2454 | 0.2891 | 0.0925 | -2.2792 |
| 7 | 22 | 0.6364 | 0.1026 | 1.3296 | 0.6940 | 0.0983 | 1.9742 |
| 8 | 80 | 0.4125 | 0.0550 | -1.5898 | 0.4121 | 0.0550 | -1.5966 |
| 9 | 145 | 0.4483 | 0.0413 | -1.2524 | 0.4460 | 0.0413 | -1.3079 |
| 10 | 110 | 0.4091 | 0.0469 | -1.9392 | 0.4076 | 0.0469 | -1.9716 |
| 11 | 128 | 0.5547 | 0.0439 | 1.2449 | 0.5561 | 0.0439 | 1.2773 |
| 12 | 57 | 0.4737 | 0.0661 | -0.3979 | 0.4727 | 0.0661 | -0.4123 |
| 13 | 138 | 0.4203 | 0.0420 | -1.8970 | 0.4200 | 0.0420 | -1.9035 |
| 14 | 94 | 0.5213 | 0.0515 | 0.4129 | 0.5228 | 0.0515 | 0.4429 |
| 15 | 138 | 0.6014 | 0.0417 | 2.4341 | 0.6079 | 0.0416 | 2.5961 |
| 18 | 135 | 0.4296 | 0.0426 | -1.6517 | 0.4290 | 0.0426 | -1.6670 |
| 19 | 130 | 0.5231 | 0.0438 | 0.5268 | 0.5231 | 0.0438 | 0.5271 |
| 20 | 135 | 0.5556 | 0.0428 | 1.2990 | 0.5556 | 0.0428 | 1.2994 |
| 21 | 110 | 0.3909 | 0.0465 | -2.3448 | 0.3531 | 0.0456 | -3.2227 |
| 23 | 104 | 0.3558 | 0.0469 | -3.0723 | 0.3555 | 0.0469 | -3.0778 |
| 24 | 137 | 0.4380 | 0.0424 | -1.4637 | 0.4368 | 0.0424 | -1.4916 |
| 25 | 144 | 0.5139 | 0.0417 | 0.3335 | 0.5151 | 0.0416 | 0.3628 |
| 26 | 124 | 0.4355 | 0.0445 | -1.4490 | 0.4352 | 0.0445 | -1.4551 |
| 27 | 68 | 0.5882 | 0.0597 | 1.4784 | 0.5883 | 0.0597 | 1.4788 |
| 28 | 131 | 0.4046 | 0.0429 | -2.2252 | 0.4042 | 0.0429 | -2.2344 |
| 29 | 143 | 0.4965 | 0.0418 | -0.0836 | 0.4965 | 0.0418 | -0.0836 |
| 30 | 25 | 0.3600 | 0.0960 | -1.4583 | 0.2918 | 0.0909 | -2.2906 |
| 31 | 21 | 0.1905 | 0.0857 | -3.6122 | 0.0364 | 0.0409 | -11.3488 |

Note: se = standard error, z-test = test of the null hypothesis that $\hat{\alpha} = 0.5$. The instruments used are the following: a constant (Model 1), a constant and the lagged exchange rate (Model 2).

Table 5: Asymmetry parameter, lin-lin loss function, twelve-months-ahead forecasts

| No. | Obs. | $\hat{\alpha}_{Model1}$ | se | z-test | $\hat{\alpha}_{Model2}$ | se | z-test |
|-----|------|-------------------------|--------|---------|-------------------------|--------|---------|
| 1 | 110 | 0.5000 | 0.0477 | 0.0000 | 0.5000 | 0.0477 | 0.0000 |
| 2 | 105 | 0.4286 | 0.0483 | -1.4790 | 0.4236 | 0.0482 | -1.5850 |
| 3 | 133 | 0.3534 | 0.0414 | -3.5372 | 0.3515 | 0.0414 | -3.5863 |
| 4 | 123 | 0.4959 | 0.0451 | -0.0902 | 0.4959 | 0.0451 | -0.0902 |
| 5 | 66 | 0.4545 | 0.0613 | -0.7416 | 0.4250 | 0.0608 | -1.2328 |
| 7 | 22 | 0.8636 | 0.0732 | 4.9701 | 0.9967 | 0.0122 | 40.6946 |
| 8 | 77 | 0.4545 | 0.0567 | -0.8010 | 0.4462 | 0.0566 | -0.9498 |
| 9 | 137 | 0.3869 | 0.0416 | -2.7190 | 0.3865 | 0.0416 | -2.7284 |
| 10 | 102 | 0.3725 | 0.0479 | -2.6623 | 0.3651 | 0.0477 | -2.8307 |
| 11 | 122 | 0.5574 | 0.0450 | 1.2759 | 0.5624 | 0.0449 | 1.3890 |
| 12 | 57 | 0.5789 | 0.0654 | 1.2072 | 0.6415 | 0.0635 | 2.2275 |
| 13 | 129 | 0.3876 | 0.0429 | -2.6204 | 0.3777 | 0.0427 | -2.8643 |
| 14 | 85 | 0.5765 | 0.0536 | 1.4268 | 0.5883 | 0.0534 | 1.6545 |
| 15 | 130 | 0.6308 | 0.0423 | 3.0895 | 0.6322 | 0.0423 | 3.1246 |
| 18 | 126 | 0.4127 | 0.0439 | -1.9905 | 0.4126 | 0.0439 | -1.9925 |
| 19 | 122 | 0.4508 | 0.0450 | -1.0917 | 0.4494 | 0.0450 | -1.1239 |
| 20 | 127 | 0.5039 | 0.0444 | 0.0887 | 0.5042 | 0.0444 | 0.0957 |
| 21 | 102 | 0.3333 | 0.0467 | -3.5707 | 0.3333 | 0.0467 | -3.5707 |
| 23 | 95 | 0.3368 | 0.0485 | -3.3647 | 0.3299 | 0.0482 | -3.5273 |
| 24 | 129 | 0.4341 | 0.0436 | -1.5099 | 0.4337 | 0.0436 | -1.5193 |
| 25 | 135 | 0.4074 | 0.0423 | -2.1895 | 0.4022 | 0.0422 | -2.3179 |
| 26 | 118 | 0.5085 | 0.0460 | 0.1841 | 0.5085 | 0.0460 | 0.1853 |
| 27 | 64 | 0.5156 | 0.0625 | 0.2501 | 0.5167 | 0.0625 | 0.2681 |
| 28 | 122 | 0.5328 | 0.0452 | 0.7258 | 0.5334 | 0.0452 | 0.7389 |
| 29 | 134 | 0.5522 | 0.0430 | 1.2161 | 0.5535 | 0.0429 | 1.2450 |

Note: se = standard error, z-test = test of the null hypothesis that $\hat{\alpha} = 0.5$. The instruments used are the following: a constant (Model 1), a constant and the lagged exchange rate (Model 2).

Table 6: J-test, lin-lin loss function, pooled data

Panel A: One-month-ahead forecasts, lin-lin loss function

| No. | Obs. | $J(0.5)$ | p | $J(\hat{\alpha})$ | p |
|-----|------|----------|--------|-------------------|--------|
| All | 2927 | 12.6112 | 0.0018 | 11.6722 | 0.0001 |

Panel B: Three-months-ahead forecasts, lin-lin loss function

| No. | Obs. | $J(0.5)$ | p | $J(\hat{\alpha})$ | p |
|-----|------|----------|--------|-------------------|--------|
| All | 2940 | 21.5126 | 0.0000 | 16.8861 | 0.0000 |

Panel C: Twelve-months-ahead forecasts, lin-lin loss function

| No. | Obs. | $J(0.5)$ | p | $J(\hat{\alpha})$ | p |
|-----|------|----------|--------|-------------------|--------|
| All | 2747 | 7.2508 | 0.0266 | 0.416 | 0.5189 |

Panel D: One-month-ahead forecasts, quad-quad loss function

| No. | Obs. | $J(0.5)$ | p | $J(\hat{\alpha})$ | p |
|-----|------|----------|-------|-------------------|--------|
| All | 2927 | 8.1484 | 0.017 | 8.3892 | 0.0038 |

Panel E: Three-months-ahead forecasts, quad-quad loss function

| No. | Obs. | $J(0.5)$ | p | $J(\hat{\alpha})$ | p |
|-----|------|----------|--------|-------------------|--------|
| All | 2940 | 8.3867 | 0.0151 | 8.4015 | 0.0037 |

Panel F: Twelve-months-ahead forecasts, quad-quad loss function

| No. | Obs. | $J(0.5)$ | p | $J(\hat{\alpha})$ | p |
|-----|------|----------|--------|-------------------|--------|
| All | 2747 | 24.5426 | 0.0000 | 23.4341 | 0.0000 |

Note: p = p-value. $J(0.5)$ denotes the J-test for a symmetric loss function. $J(\hat{\alpha})$ denotes the J-test for an estimated lin-lin loss function. The instruments used are a constant and the lagged exchange rate.

Table 7: J-test, lin-lin loss function, one-month-ahead forecasts

| No. | Obs. | $J(0.5)$ | p | $J(\hat{\alpha})$ | p |
|-----|------|----------|--------|-------------------|--------|
| 1 | 119 | 2.0756 | 0.3542 | 0.1840 | 0.6680 |
| 2 | 104 | 2.2872 | 0.3187 | 2.1420 | 0.1433 |
| 3 | 144 | 0.7227 | 0.6967 | 0.0275 | 0.8683 |
| 4 | 129 | 2.8098 | 0.2454 | 0.0111 | 0.9161 |
| 5 | 39 | 3.1674 | 0.2052 | 0.0807 | 0.7764 |
| 6 | 26 | 0.9015 | 0.6371 | 0.6985 | 0.4033 |
| 7 | 21 | 5.3776 | 0.0680 | 4.0021 | 0.0454 |
| 8 | 79 | 0.6135 | 0.7358 | 0.6037 | 0.4372 |
| 9 | 147 | 1.0840 | 0.5816 | 0.7527 | 0.3856 |
| 10 | 107 | 0.7310 | 0.6938 | 0.6436 | 0.4224 |
| 11 | 129 | 5.9054 | 0.0522 | 5.4514 | 0.0196 |
| 12 | 57 | 0.2852 | 0.8671 | 0.1303 | 0.7181 |
| 13 | 140 | 0.8801 | 0.6440 | 0.4205 | 0.5167 |
| 14 | 96 | 0.7719 | 0.6798 | 0.1035 | 0.7477 |
| 15 | 140 | 8.1282 | 0.0172 | 7.0398 | 0.0080 |
| 18 | 137 | 0.3558 | 0.8370 | 0.1721 | 0.6782 |
| 19 | 132 | 5.1232 | 0.0772 | 0.0021 | 0.9631 |
| 20 | 133 | 3.2451 | 0.1974 | 0.5191 | 0.4712 |
| 21 | 111 | 14.3353 | 0.0008 | 13.3444 | 0.0003 |
| 23 | 106 | 2.5793 | 0.2754 | 0.7098 | 0.3995 |
| 24 | 139 | 0.7561 | 0.6852 | 0.5822 | 0.4455 |
| 25 | 146 | 6.3402 | 0.0420 | 4.0303 | 0.0447 |
| 26 | 124 | 1.2613 | 0.5322 | 0.9619 | 0.3267 |
| 27 | 66 | 1.2175 | 0.5440 | 0.6870 | 0.4072 |
| 28 | 132 | 3.2928 | 0.1927 | 0.2704 | 0.6031 |
| 29 | 144 | 0.2263 | 0.8930 | 0.1154 | 0.7340 |
| 30 | 27 | 5.7175 | 0.0573 | 1.3510 | 0.2451 |
| 31 | 23 | 4.9921 | 0.0824 | 1.6648 | 0.1970 |

Note: p = p-value. $J(0.5)$ denotes the J-test for a symmetric loss function. $J(\hat{\alpha})$ denotes the J-test for an estimated lin-lin loss function. The instruments used are a constant and the lagged exchange rate.

Table 8: J-test, lin-lin loss function, three-months-ahead forecasts

| No. | Obs. | $J(0.5)$ | p | $J(\hat{\alpha})$ | p |
|-----|------|----------|--------|-------------------|--------|
| 1 | 117 | 2.0092 | 0.3662 | 0.9642 | 0.3261 |
| 2 | 114 | 1.5281 | 0.4658 | 1.5281 | 0.2164 |
| 3 | 142 | 3.6948 | 0.1576 | 1.7959 | 0.1802 |
| 4 | 127 | 1.0020 | 0.6059 | 0.0493 | 0.8243 |
| 5 | 66 | 1.0084 | 0.6040 | 1.0084 | 0.3153 |
| 6 | 24 | 4.3362 | 0.1144 | 0.1476 | 0.7008 |
| 7 | 22 | 5.2695 | 0.0717 | 3.6106 | 0.0574 |
| 8 | 80 | 2.6209 | 0.2697 | 0.1646 | 0.6850 |
| 9 | 145 | 4.5934 | 0.1006 | 3.0456 | 0.0810 |
| 10 | 110 | 4.4851 | 0.1062 | 0.8741 | 0.3498 |
| 11 | 128 | 3.0976 | 0.2125 | 1.6057 | 0.2051 |
| 12 | 57 | 1.1138 | 0.5730 | 0.9946 | 0.3186 |
| 13 | 138 | 3.7382 | 0.1543 | 0.2274 | 0.6334 |
| 14 | 94 | 3.2768 | 0.1943 | 3.1732 | 0.0749 |
| 15 | 138 | 9.6045 | 0.0082 | 4.1450 | 0.0418 |
| 18 | 135 | 3.2759 | 0.1944 | 0.6089 | 0.4352 |
| 19 | 130 | 0.3152 | 0.8542 | 0.0388 | 0.8438 |
| 20 | 135 | 1.6873 | 0.4301 | 0.0207 | 0.8857 |
| 21 | 110 | 20.8413 | 0.0000 | 14.8317 | 0.0001 |
| 23 | 104 | 8.7453 | 0.0126 | 0.0850 | 0.7706 |
| 24 | 137 | 3.3703 | 0.1854 | 1.2633 | 0.2610 |
| 25 | 144 | 5.9325 | 0.0515 | 5.8195 | 0.0158 |
| 26 | 124 | 2.3205 | 0.3134 | 0.2593 | 0.6106 |
| 27 | 68 | 2.1263 | 0.3454 | 0.0090 | 0.9245 |
| 28 | 131 | 5.0205 | 0.0812 | 0.2625 | 0.6084 |
| 29 | 143 | 0.0089 | 0.9955 | 0.0019 | 0.9649 |
| 30 | 25 | 6.4049 | 0.0407 | 4.6600 | 0.0309 |
| 31 | 21 | 12.5172 | 0.0019 | 17.7197 | 0.0000 |

Note: p = p-value. $J(0.5)$ denotes the J-test for a symmetric loss function. $J(\hat{\alpha})$ denotes the J-test for an estimated lin-lin loss function. The instruments used are a constant and the lagged exchange rate.

Table 9: J-test, lin-lin loss function, twelve-months-ahead forecasts

| No. | Obs. | $J(0.5)$ | p | $J(\hat{\alpha})$ | p |
|-----|------|----------|--------|-------------------|--------|
| 1 | 110 | 0.7140 | 0.6998 | 0.7140 | 0.3981 |
| 2 | 105 | 5.6399 | 0.0596 | 3.4476 | 0.0633 |
| 3 | 133 | 12.3538 | 0.0021 | 0.8330 | 0.3614 |
| 4 | 123 | 0.0082 | 0.9959 | 0.0000 | 0.9947 |
| 5 | 66 | 12.6312 | 0.0018 | 13.2406 | 0.0003 |
| 7 | 22 | 15.1782 | 0.0005 | 121.8138 | 0.0000 |
| 8 | 77 | 6.7831 | 0.0337 | 5.9958 | 0.0143 |
| 9 | 137 | 7.2471 | 0.0267 | 0.2231 | 0.6367 |
| 10 | 102 | 9.2931 | 0.0096 | 2.8559 | 0.0910 |
| 11 | 122 | 6.4840 | 0.0391 | 4.9082 | 0.0267 |
| 12 | 57 | 17.6776 | 0.0001 | 13.5675 | 0.0002 |
| 13 | 129 | 12.0546 | 0.0024 | 5.2564 | 0.0219 |
| 14 | 85 | 6.9824 | 0.0305 | 5.7491 | 0.0165 |
| 15 | 130 | 9.5722 | 0.0083 | 0.6803 | 0.4095 |
| 18 | 126 | 3.9044 | 0.1420 | 0.0626 | 0.8025 |
| 19 | 122 | 2.9015 | 0.2344 | 1.7295 | 0.1885 |
| 20 | 127 | 4.6024 | 0.1001 | 4.5895 | 0.0322 |
| 21 | 102 | 11.3333 | 0.0035 | 0.0000 | 0.9992 |
| 23 | 95 | 12.4373 | 0.0020 | 1.9722 | 0.1602 |
| 24 | 129 | 2.6393 | 0.2672 | 0.3926 | 0.5310 |
| 25 | 135 | 8.4897 | 0.0143 | 3.6213 | 0.0570 |
| 26 | 118 | 0.4032 | 0.8174 | 0.3711 | 0.5424 |
| 27 | 64 | 2.2281 | 0.3282 | 2.1421 | 0.1433 |
| 28 | 122 | 1.5920 | 0.4511 | 1.0725 | 0.3004 |
| 29 | 134 | 3.0029 | 0.2228 | 1.5403 | 0.2146 |

Note: p = p-value. $J(0.5)$ denotes the J-test for a symmetric loss function. $J(\hat{\alpha})$ denotes the J-test for an estimated lin-lin loss function. The instruments used are a constant and the lagged exchange rate.